

Solution

PREBOARD EXAM- 2 2025-26

Class 10 - Mathematics

Section A

1.
(c) irrational number
Explanation:
Here, 3 is rational and $2\sqrt{5}$ is irrational.
We know that the sum of a rational and an irrational is an irrational number, therefore, $3 + 2\sqrt{5}$ is irrational.
2.
(b) $a < 0$, $b < 0$ and $c > 0$
Explanation:
Clearly, $f(x) = ax^2 + bx + c$ represent a parabola opening downwards.
Clearly $a < 0$
Let, $y = ax^2 + bx + c$ cuts y-axis at P which lies on OY.
Putting $x = 0$ in $y = ax^2 + bx + c$, we get $y = c$. So the coordinates of P are $(0, c)$.
Clearly, P lies on OY. Therefore $c > 0$
The vertex $\left(\frac{-b}{2a}, \frac{-D}{4a}\right)$ of the parabola is in the second quadrant.
Therefore, $\frac{-b}{2a} < 0$, $b < 0$
Therefore $a < 0$, $b < 0$ and $c > 0$.
3. (a) 0
Explanation:
The number of solutions of two linear equations representing parallel lines is 0 because two linear equations representing parallel lines has no solution and they are inconsistent.
4.
(c) $b^2 - 4ac$
Explanation:
Discriminant of the quadratic equation $ax^2 + bx + c = 0$ is $D = b^2 - 4ac$
5. (a) Gauss
Explanation:
The famous mathematician associated with finding the sum of the first 100 natural numbers is Gauss.
Gauss noticed that if he was to split the numbers into two groups (1 to 50 and 51 to 100), he could add them together vertically to get a sum of 101. **Gauss** realized then that his final total would be $50(101) = 5050$.
6.
(d) 5 units
Explanation:
According to question,
Coordinates of Chaitanya's house are (6, 5)
Coordinates of Hamida's house are (2, 2)
 \therefore Shortest distance between their houses
 $= \sqrt{(6-2)^2 + (5-2)^2} = 5$ units.
7.
(b) (3, 0)
Explanation:

Required coordinates are

$$= \left(\frac{(1 \times 6 + 3 \times 2)}{(1+3)}, \frac{(1 \times (-9) + 3 \times 3)}{(1+3)} \right)$$

$$= \left(\frac{12}{4}, 0 \right)$$

$$= (3, 0)$$

8.

(b) 16 cm

Explanation:

$$\triangle PSR \sim \triangle PRQ \text{ (AA Similarity)} \Rightarrow \frac{4}{8} = \frac{8}{PQ} \Rightarrow PQ = 16 \text{ cm}$$

9.

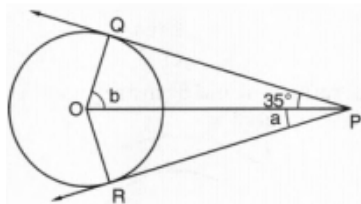
(d) $a = 35^\circ$, $b = 55^\circ$

Explanation:

In the figure, PQ and PR are the tangents drawn from P to the circle with centre O

$$\angle OPQ = 35^\circ$$

PO is joined



$PQ = PR$ (tangents from P to the circle)

$$\angle OPQ = \angle OPR$$

$$\Rightarrow 35^\circ = a$$

$$\Rightarrow a = 35^\circ$$

OQ is radius and PQ is tangent $OQ \perp PQ$

$$\Rightarrow \angle OQP = 90^\circ$$

In $\triangle OQP$

$$\angle POQ + \angle QPO = 90^\circ$$

$$\Rightarrow b + 35^\circ = 90^\circ$$

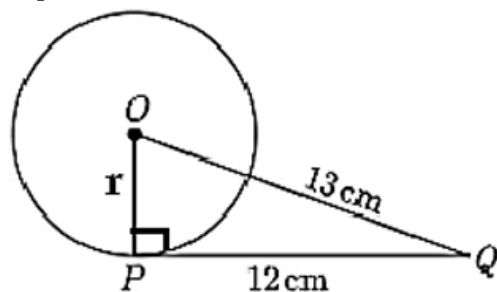
$$\Rightarrow b = 90^\circ - 35^\circ = 55^\circ$$

$$a = 35^\circ, b = 55^\circ$$

10.

(d) 5

Explanation:



\therefore We know that

$$PQ \perp OP$$

$\therefore \triangle QPO$ is right angled \triangle

\therefore By pythag theory.

$$OQ^2 = QP^2 + OP^2$$

$$(13)^2 = (12)^2 + OP^2$$

$$r^2 = 169 - 144.$$

$$r^2 = 25$$

$$r = 5 \text{ cm}$$

11. (a) $\operatorname{cosec} \alpha$

Explanation:

$$1 + \frac{\cot^2 \alpha}{1 + \operatorname{cosec} \alpha}$$

$$= 1 + \frac{\operatorname{cosec}^2 \alpha - 1}{1 + \operatorname{cosec} \alpha}$$

$$= 1 + \frac{(\operatorname{cosec} \alpha - 1)(\operatorname{cosec} \alpha + 1)}{1 + \operatorname{cosec} \alpha}$$

$$= 1 + \operatorname{cosec} \alpha - 1 = \operatorname{cosec} \alpha$$

12.

(b) 60°

Explanation:

$$\sin^2 \theta = \frac{3}{4}$$

$$\sin \theta = \frac{\sqrt{3}}{2}$$

$$\sin \theta = \sin 60^\circ$$

$$\theta = 60^\circ$$

13.

(b) $\frac{40}{\sqrt{3}} \text{ m}$

Explanation:

$$\frac{40}{\sqrt{3}} \text{ m}$$

14.

(d) 112 cm^2

Explanation:

For Triangle POS,

$$PO = OS = 14 \text{ cm}$$

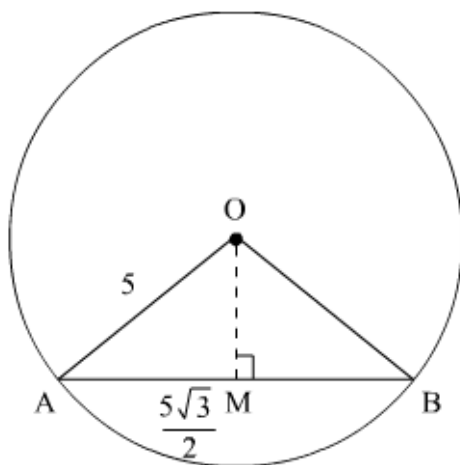
Now Get PS by pythagoras theorem.

$$\text{Again, Required area} = \frac{1}{4} \text{ Area of Circle} - \text{Area POS}$$

15. (a) $\frac{25\pi}{3} \text{ cm}^2$

Explanation:

We have to find the area of the sector OAB.



We have,

$$AM = \frac{5\sqrt{3}}{2}$$

So,

$$\sin \angle AOM = \frac{5\sqrt{3}}{2(5)}$$

Hence,

$$\angle AOM = 60^\circ$$

$$\Rightarrow \angle AOB = 120^\circ$$

$$\text{Area of sector AOB} = \frac{120}{360} \times \pi \times 5^2 \text{ cm}^2 = \frac{25\pi}{3} \text{ cm}^2$$

16.

(d) $\frac{5}{11}$

Explanation:

Total number of fish = 15 + 18 = 33

Male fish = 15

Number of possible outcomes = 15

Number of total outcomes = 15 + 18 = 33

$$\text{Required Probability} = \frac{15}{33} = \frac{5}{11}$$

17. (a) $\frac{1}{365}$

Explanation:

Assuming a non-leap year

Ram can have the birthday on any day of the 365 days of the year

Shyam has a different birthday if his birthday is on any of the remaining 364 days of the year

$$\text{Therefore } P(\text{Ram and Shyam have different birthdays}) = \frac{364}{365}$$

and so, $P(\text{Ram and Shyam have birthdays on the same day}) = 1 - P(\text{Ram and Shyam have different birthdays})$

$$= 1 - \frac{364}{365}$$

$$= \frac{1}{365}$$

18.

(b) 6

Explanation:

Here Observations 5 and 6 has more frequency than those of other numbers that is 3

But here it is given that mode is 6,

\therefore 6 could repeat itself at least once more.

\Rightarrow x should be 6.

19. (a) Both A and R are true and R is the correct explanation of A.

Explanation:

Both A and R are true and R is the correct explanation of A.

20.

(c) A is true but R is false.

Explanation:

A is true but R is false.

Section B

21. We have to find the greatest number which divides 85 and 72 leaving remainder 1 and 2 respectively.

Let assume that x be the greatest number which divides 85 and 72 leaving remainder 1 and 2 respectively.

So, it means

$$x \text{ divides } 85 - 1 = 84$$

and

$$x \text{ divides } 72 - 2 = 70$$

So, from this we concluded that

$$= x \text{ divides } 84 \text{ and } 70$$

$$= x = \text{HCF}(84, 70)$$

Now, to find HCF(84, 70), we use method of prime factorization.

$$\text{Prime factors of } 84 = 2 \times 2 \times 3 \times 7$$

Prime factors of $70 = 2 \times 5 \times 7$

So,

$$= \text{HCF}(84, 70) = 2 \times 7 = 14$$

$$= x = 14$$

Hence, 14 is the greatest number which divides 85 and 72 leaving remainder 1 and 2 respectively.

22. Given: In the figure, ABC and AMP are two right triangles, right angled at B and M respectively,

To prove:

$$\text{i. } \triangle ABC \sim \triangle AMP$$

$$\text{ii. } \frac{CA}{PA} = \frac{BC}{MP}$$

Proof:

$$\text{i. In } \triangle ABC \sim \triangle AMP$$

$$\angle ABC = \angle AMP \text{ (1) [Each equal to } 90^\circ]$$

$$\angle BAC = \angle MAP \text{ (2) [Common angle]}$$

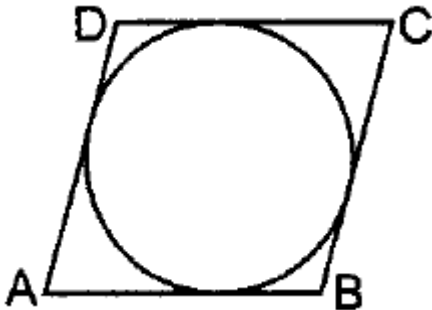
In view of (1) and (2)

$$\triangle ABC \sim \triangle AMP \text{ AA similarity criterion}$$

$$\text{ii. } \triangle ABC \sim \triangle AMP \text{ Proved above in (i)}$$

$$\therefore \frac{CA}{PA} = \frac{BC}{MP} \text{ Corresponding sides of two similar triangles are proportional.}$$

23. Let ABCD be the quadrilateral circumscribing the circle with centre O. The quadrilateral touches the circle at points P, Q, R, S.



To prove: $AB + CD = AD + BC$

proof: lengths of tangents drawn from an external point are equal

$$\text{Hence, } AP = AS \text{ ... (i)}$$

$$BP = BQ \text{ ... (ii)}$$

$$CR = CQ \text{ ... (iii)}$$

$$DR = DS \text{ ... (iv)}$$

Adding (i) + (ii) + (iii) + (iv), we get

$$AB + BP + CR + DR = AS + BQ + CQ + DS$$

$$AB + CD = AD + BC$$

Hence proved

$$24. \text{ We have } \frac{\cos(45^\circ)}{\sec(30^\circ) + \csc(30^\circ)}$$

$$= \frac{\frac{1}{\sqrt{2}}}{\frac{2}{\sqrt{3}} + 2}$$

$$= \frac{\frac{1}{\sqrt{2}}}{2\left(\frac{1}{\sqrt{3}} + 1\right)}$$

$$= \frac{1}{2\sqrt{2}\left(\frac{1+\sqrt{3}}{\sqrt{3}}\right)}$$

$$= \frac{\sqrt{3}}{2\sqrt{2}(1+\sqrt{3})}$$

it is clear that the denominator has an irrational number, we need to rationalize it, we get

$$= \frac{\sqrt{3}}{2\sqrt{2}(1+\sqrt{3})} \times \frac{\sqrt{2}(1-\sqrt{3})}{\sqrt{2}(1-\sqrt{3})}$$

$$= \frac{\sqrt{2}(\sqrt{3}-3)}{2(2)(1^2-(\sqrt{3})^2)}$$

$$= \frac{\sqrt{6}-3\sqrt{2}}{4(1-3)}$$

$$= \frac{\sqrt{6}-3\sqrt{2}}{4(-2)}$$

$$= \frac{\sqrt{6}-3\sqrt{2}}{-8}$$

$$= \frac{3\sqrt{2}-\sqrt{6}}{8}$$

OR

$$\begin{aligned} \text{LHS} &= \frac{\tan^2 A}{1+\tan^2 A} + \frac{\cot^2 A}{1+\cot^2 A} \\ &= \frac{\tan^2 A}{\sec^2 A} + \frac{\cot^2 A}{1+\cot^2 A} \\ &= \frac{\sin^2 A}{\cos^2 A} + \frac{\cos^2 A}{\sin^2 A} \\ &= \frac{1}{\cos^2 A} + \frac{1}{\sin^2 A} \\ &= \frac{\sin^2 A}{\cos^2 A} \times \frac{\cos^2 A}{1} + \frac{\cos^2 A}{\sin^2 A} \times \frac{\sin^2 A}{1} \\ &= \sin^2 A + \cos^2 A \\ &= 1 \quad [\because \sin^2 A + \cos^2 A = 1] \\ &= \text{RHS} \end{aligned}$$

Hence proved.

$$25. \text{Area of first sector} = \left(\frac{1}{2}\right) (r_1)^2 \theta_1,$$

where r_1 is the radius,

θ_1 is the angle in radians subtended by the arc at the center of the circle.

$$\text{Area of second sector} = \left(\frac{1}{2}\right) (r_2)^2 \theta_2$$

where r_2 is the radius,

θ_2 is the angle in radians subtended by the arc at the center of the circle.

$$\text{Given that: } \left(\frac{1}{2}\right) (r_1)^2 \theta_1 = \left(\frac{1}{2}\right) (r_2)^2 \theta_2$$

$$\Rightarrow (r_1)^2 \theta_1 = (r_2)^2 \theta_2$$

It depends on both radius and angle subtended at the center. But arc length only depends on radius of the circle. Therefore, it is not necessary that the corresponding arc lengths are equal. It is possible only if corresponding angles are equal (because then, the corresponding radii will be equal and hence the arc lengths will be equal).

OR



$$\text{Given Radius} = r = 5\sqrt{2}\text{cm}$$

$$= OA = OB$$

$$\text{Length of chord AB} = 10 \text{ cm}$$

$$\text{In } \triangle OAB, OA = OB = 5\sqrt{2}$$

$$AB = 10\text{cm}$$

$$OA^2 + OB^2 = (5\sqrt{2})^2 + (5\sqrt{2})^2$$

$$= 50 + 50 = 100 = (AB)^2$$

Pythagoras theorem is satisfied $\triangle OAB$ is right triangle

$$= \text{angle subtended by chord} = \angle AOB = 90^\circ$$

Area of segment (minor) = shaded region

$$= \text{area of sector} - \text{area of } \triangle OAB$$

$$= \frac{\theta}{360} \times \pi r^2 - \frac{1}{2} \times OA \times OB$$

$$= \frac{90}{360} \times \frac{22}{7} (5\sqrt{2})^2 - \frac{1}{2} \times 5\sqrt{2} \times 5\sqrt{2}$$

$$= \frac{275}{7} - 25 = \frac{100}{7} \text{cm}^2$$

Area of major segment = (area of circle) - (area of minor segment)

$$= \pi r^2 - \frac{100}{7}$$

$$= \frac{22}{7} \times (5\sqrt{2})^2 - \frac{100}{7}$$

$$= \frac{1100}{7} - \frac{100}{7}$$

$$= \frac{1000}{7} \text{cm}^2$$

Section C

26. We have,

$$60 = 2^2 \times 3 \times 5$$

$$168 = 2^3 \times 3 \times 7$$

$$330 = 2 \times 3 \times 5 \times 11$$

$$\text{HCF} = 6$$

They can put 6 food items in 1 packet.

$$\text{so the number of packets required for 60 pieces of pastries} = \frac{60}{6} = 10$$

$$\text{the number of packets required for 168 pieces of cookies} = \frac{168}{6} = 28$$

$$\text{the number of packets required for 330 chocolate bars} = \frac{330}{6} = 55$$

$$\text{Total Packets required} = 10 + 28 + 55 = 93$$

27. Given polynomial is

$$f(x) = x^2 - 2x + 3$$

Compare with $ax^2 + bx + c$, we get

$$a = 1, b = -2 \text{ and } c = 3$$

$$\text{Sum of the zeroes} = \alpha + \beta = -\frac{b}{a} = -\frac{-2}{1} = 2$$

$$\text{Product of the zeroes} = \alpha\beta = \frac{c}{a} = \frac{3}{1} = 3$$

$$\text{i. Sum of the zeroes of new polynomial} = (\alpha + 2) + (\beta + 2)$$

$$= \alpha + \beta + 4$$

$$= 2 + 4 = 6$$

$$\text{Product of the zeroes of new polynomial} = (\alpha + 2)(\beta + 2)$$

$$= \alpha\beta + 2\alpha + 2\beta + 4$$

$$= \alpha\beta + 2(\alpha + \beta) + 4$$

$$= 3 + 2(2) + 4$$

$$= 11$$

$$\text{So, quadratic polynomial is: } x^2 - (\text{sum of the zeroes})x + (\text{product of the zeroes})$$

$$= x^2 - 6x + 11$$

$$\text{Hence, the required quadratic polynomial is } f(x) = (x^2 - 6x + 11)$$

$$\text{ii. Sum of the zeroes of new polynomial} = \frac{\alpha-1}{\alpha+1} + \frac{\beta-1}{\beta+1}$$

$$= \frac{(\alpha-1)(\beta+1) + (\beta-1)(\alpha+1)}{(\alpha+1)(\beta+1)}$$

$$= \frac{\alpha\beta + \alpha - \beta - 1 + \alpha\beta + \beta - \alpha - 1}{(\alpha+1)(\beta+1)}$$

$$= \frac{\alpha\beta - 1 + \alpha\beta - 1}{\alpha\beta + \alpha + \beta + 1}$$

$$= \frac{3 - 1 + 3 - 1}{3 + 1 + 2}$$

$$= \frac{4}{6}$$

$$= \frac{2}{3}$$

$$\text{Product of the zeroes of new polynomial} = \frac{\alpha-1}{\alpha+1} \times \frac{\beta-1}{\beta+1}$$

$$= \frac{(\alpha-1)(\beta-1)}{(\alpha+1)(\beta+1)}$$

$$= \frac{\alpha\beta - \alpha - \beta + 1}{\alpha\beta + \alpha + \beta + 1}$$

$$= \frac{\alpha\beta - (\alpha + \beta) + 1}{\alpha\beta + (\alpha + \beta) + 1}$$

$$= \frac{3 - 2 + 1}{3 + 2 + 1}$$

$$= \frac{2}{6} = \frac{1}{3}$$

$$\text{So, the quadratic polynomial is, } x^2 - (\text{sum of the zeroes})x + (\text{product of the zeroes})$$

$$= x^2 - \frac{2}{3}x + \frac{1}{3}$$

$$\text{Thus, the required quadratic polynomial is } f(x) = k \left(x^2 - \frac{2}{3}x + \frac{1}{3} \right).$$

28. Let the fixed charge for first three days be $Rs. x$

The additional charge for each day thereafter be $Rs. y$.

Then according to question, we have

$$x + 4y = 22 \dots(i)$$

$$x + 2y = 16 \dots(ii)$$

Subtracting equation (ii) from (i),

$$2y = 6$$

$$\Rightarrow y = 3$$

Substituting $y = 3$ in (ii),

$$x + 2(3) = 16$$

$$\Rightarrow x + 6 = 16$$

$$\Rightarrow x = 10$$

Thus, the fixed charge for first three days is Rs. 10.

and the additional charge for each day thereafter is Rs.3.

OR

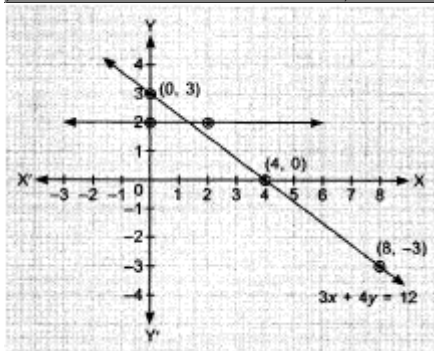
Given equations are $3x + 4y = 12$ and $y = 2$

Solution table for $3x + 4y = 12$ is

x	0	4	8
y	3	0	-3

Table for $y = 2$ is

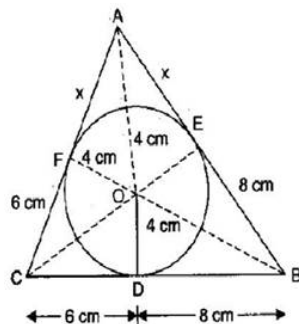
x	0	1	2
y	2	2	2



\therefore Lines intersect at one point $(\frac{4}{3}, 2)$

\Rightarrow Pair of linear equations has a unique solution.

29. Join OE and OF. Also join OA, OB and OC.



Since $BD = 8$ cm

$\therefore BE = 8$ cm

[Tangents from an external point to a circle are equal]

Since $CD = 6$ cm

$\therefore CF = 6$ cm

[Tangents from an external point to a circle are equal]

Let $AE = AF = x$

Since $OD = OE = OF = 4$ cm [Radii of a circle are equal]

\therefore Semi-perimeter of $\triangle ABC = \frac{(x+6)(x+8) + (6+8)}{2} = \frac{(2x+28)}{2} = (x+14)$ cm

\therefore Area of $\triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$

$$= \sqrt{(x+14)(x+14-14)(x+14-x+8)(x+14-x+6)}$$

$$= \sqrt{(x+14)(x)(8)(6)} \text{ cm}^2$$

Now, Area of $\triangle ABC$ = Area of $\triangle OBC$ + Area of $\triangle OCA$ + Area of $\triangle OAB$

$$\Rightarrow \sqrt{(x+14)(x)(8)(6)} = \frac{(6+8)x}{2} + \frac{(x+6)4}{2} + \frac{(x+8)4}{2}$$

$$\Rightarrow \sqrt{(x+14)(x)(8)(6)} = 28 + 2x + 12 + 2x + 16$$

$$\Rightarrow \sqrt{(x+14)(x)(8)(6)} = 4x + 56$$

$$\Rightarrow \sqrt{(x+14)(x)(8)(6)} = 4(x+14)$$

Squaring both sides,

$$(x+14)(x)(6)(8) = 16(x+14)^2$$

$$\Rightarrow 3x = x + 14$$

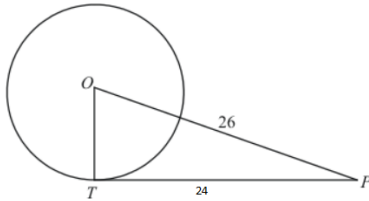
$$\Rightarrow 2x = 14$$

$$\Rightarrow x = 7$$

$$\therefore AB = x + 8 = 7 + 8 = 15 \text{ cm}$$

$$\text{And } AC = x + 6 = 7 + 6 = 13 \text{ cm}$$

OR



Construction: Join OT

We know that the radius and tangent are perpendicular at their point of contact.

In right triangle OTP

According to Pythagoras theorem, we get

$$OP^2 = OT^2 + TP^2$$

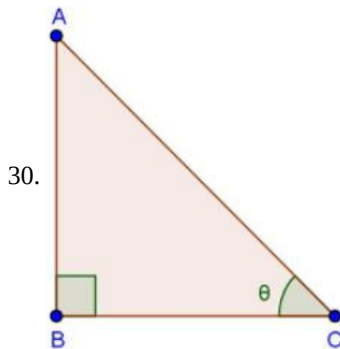
$$\Rightarrow 26^2 = TO^2 + 24^2$$

$$\Rightarrow 676 = TO^2 + 576$$

$$\Rightarrow TO^2 = 100$$

$$\Rightarrow TO = 10 \text{ cm}$$

Therefore, the radius of the circle is equal to 10 cm.



$$\text{Given } \cos \theta = \frac{12}{13} = \frac{BC}{AC}$$

$$\text{Let } BC = 12K$$

$$\text{and, } AC = 13K$$

In $\triangle ABC$, By Pythagoras theorem

$$AB^2 + BC^2 = AC^2$$

$$AB^2 + (12K)^2 = (13K)^2$$

$$AB^2 + 144K^2 = 169K^2$$

$$AB^2 = 169K - 144K^2 = 25K^2$$

$$AB = \sqrt{25K^2} = 5K$$

$$\therefore \sin \theta = \frac{AB}{AC} = \frac{5K}{13K} = \frac{5}{13}$$

$$\tan \theta = \frac{AB}{BC} = \frac{5K}{12K} = \frac{5}{12}$$

$$\therefore LHS = \sin \theta (1 - \tan \theta)$$

$$\begin{aligned}
&= \frac{5}{13} \left(1 - \frac{5}{12} \right) \\
&= \frac{5}{13} \left(\frac{12-5}{12} \right) \\
&= \frac{5}{13} \times \frac{7}{12} \\
&= \frac{35}{156} = RHS
\end{aligned}$$

31.

Class Interval	Frequency(f_i)	Class mark x_i	Deviation $d_i = (x_i - A) = (x_i - 57)$	$(f_i \times d_i)$
50 - 52	18	51	-6	-108
52 - 54	21	53	-4	-84
54 - 56	17	55	-2	-34
56 - 58	28	57 = A	0	0
58 - 60	16	59	2	32
60 - 62	35	61	4	140
62 - 64	15	63	6	90
	$\Sigma f_i = 150$			$\Sigma (f_i \times d_i) = 36$

Let the assumed mean $A = 57$

$$\begin{aligned}
\therefore \bar{x} &= A + \frac{\Sigma(f_i \times d_i)}{\Sigma f_i} \\
&= \left(57 + \frac{36}{150} \right) \\
&= 57 + 0.24 \\
&= 57.24
\end{aligned}$$

Hence, mean weight = 57.24 kg

Section D

32. Let the larger number be x . Then,

Square of the smaller number = $4x$

Also, Square of the larger number = x^2

It is given that the difference of the squares of the numbers is 45.

$$\therefore x^2 - 4x = 45$$

$$\Rightarrow x^2 - 4x - 45 = 0$$

$$\Rightarrow x^2 - 9x + 5x - 45 = 0$$

$$\Rightarrow x(x - 9) + 5(x - 9) = 0$$

$$\Rightarrow x - 9 = 0 \text{ or, } x + 5 = 0 \Rightarrow x = 9, -5$$

Case I When $x = 9$: In this case, we have

Square of the smaller number = $4x = 36$

\therefore Smaller number = ± 6 .

Thus, the numbers are 9, 6 or 9, -6

CASE II When $x = -5$: In this case, we have

Square of the smaller number = $4x = -20$. But, square of a number is always positive. Therefore, $x = -5$ is not possible.

Hence, the numbers are 9, 6 or 9, -6.

OR

In equation $(m + 1)y^2 - 6(m + 1)y + 3(m + 9) = 0$

$A = m + 1$, $B = -6(m + 1)$, $C = 3(m + 9)$

For equal roots, $D = B^2 - 4AC = 0$

$$36(m + 1)^2 - 4(m + 1) \times 3(m + 9) = 0$$

$$\Rightarrow 3(m^2 + 2m + 1) - (m + 1)(m + 9) = 0$$

$$\Rightarrow 2m^2 - 4m - 6 = 0$$

$$\Rightarrow m^2 - 2m - 3 = 0$$

$$\Rightarrow m^2 - 3m + m - 3 = 0$$

$$\Rightarrow m(m - 3) + 1(m - 3) = 0$$

$$\Rightarrow (m - 3)(m + 1) = 0$$

$$\therefore m = -1, 3$$

Neglecting $m \neq -1$

$$\therefore m = 3$$

$$\therefore \text{the equation becomes } 4y^2 - 24y + 36 = 0$$

$$\Rightarrow y^2 - 6y + 9 = 0$$

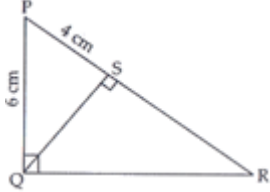
$$\Rightarrow (y - 3)(y - 3) = 0$$

$$\Rightarrow (y - 3) = 0 \quad \text{and} \quad (y - 3) = 0$$

$$\therefore \text{roots are } y = 3, 3$$

33. Given: According to the question, PQR is a right triangle right angled at Q and $QS \perp PR$. $PQ = 6$ cm and $PS = 4$ cm

To find : Length of QS, RS and QR.



In ΔPQR , $\angle PQR = 90^\circ$

and $QS \perp PR$

So, $\Delta PSQ \sim \Delta PQR$ (By AA similarity)

$$\text{Thus, } \frac{PS}{QS} = \frac{QS}{SR}$$

$$\therefore QS^2 = PS \cdot SR \dots\dots\dots(i)$$

In ΔPQS ,

$$QS^2 = PQ^2 - PS^2 \text{ [By Pythagoras theorem]}$$

$$= 6^2 - 4^2 = 36 - 16$$

$$\Rightarrow QS^2 = 20$$

$$\Rightarrow QS = 2\sqrt{5} \text{ cm}$$

Now $QS^2 = PS \cdot SR$ [From eqn(i)]

$$\Rightarrow (2\sqrt{5})^2 = 4 \times SR$$

$$\Rightarrow \frac{20}{4} = SR$$

$$\Rightarrow SR = 5 \text{ cm}$$

Now, $QS \perp SR$

$$\therefore \angle QSR = 90^\circ$$

$$\Rightarrow QR^2 = QS^2 + SR^2 \text{ [By Pythagoras theorem]}$$

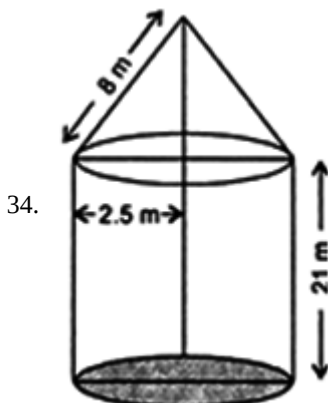
$$\Rightarrow QR^2 = (2\sqrt{5})^2 + 5^2$$

$$\Rightarrow QR^2 = 20 + 25$$

$$\Rightarrow QR^2 = 45$$

$$\Rightarrow QR = 3\sqrt{5} \text{ cm}$$

Hence, $QS = 2\sqrt{5}$ cm, $RS = 5$ cm and $QR = 3\sqrt{5}$ cm.



Radius of cylinder, $r = 2.5$ m, height of cylinder, $h = 21$ m, slant height of cone, $l = 8$ m

$$\begin{aligned}
\text{Total surface area of rocket} &= \text{Curved of cylinder} + \text{Area of base} + \text{Curved surface area of cone} \\
&= 2\pi rh + \pi r^2 + \pi rl \\
&= \pi r (2h + r + l) \\
&= \frac{22}{7} \times 2.5 (2 \times 21 + 2.5 + 8) \\
&= \frac{22}{7} \times 2.5 \times 52.5 \\
&= 412.5 \text{ m}^2
\end{aligned}$$

OR

Height of the cylinder = 3 m.

Total height of the tent above the ground = 13.5 m

height of the cone = (13.5 - 3)m = 10.5 m

Radius of the cylinder = radius of cone = 14 m

$$\text{Curved surface area of the cylinder} = 2\pi rh \text{ m}^2 = \left(2 \times \frac{22}{7} \times 14 \times 3\right) \text{ m}^2 = 264 \text{ m}^2$$

$$\therefore l = \sqrt{r^2 + h^2} = \sqrt{14^2 + (10.5)^2} = \sqrt{196 + 110.25} = \sqrt{306.25} = 17.5$$

$$\therefore \text{Cured surface area of the cone} = \pi rl = \left(\frac{22}{7} \times 14 \times 17.5\right) \text{ m}^2 = 770 \text{ m}^2$$

Let S be the total area which is to be painted. Then,

S = Curved surface area of the cylinder + Curved surface area of the cone

$$\Rightarrow S = (264 + 770) \text{ m}^2 = 1034 \text{ m}^2$$

Hence, Cost of painting = S × Rate = ₹ (1034 × 2) = ₹ 2068

35.	Class Interval	Mid - value	$d_i = x_i - 15$	$u_i = \frac{(x_i - 15)}{6}$	Frequency f_i	$f_i u_i$
	0 – 6	3	-12	-2	-1	-14
	6 – 12	9	-6	-1	5	-5
	12 – 18	15	0	0	10	0
	18 – 24	21	6	1	12	12
	24 – 30	27	12	2	6	12
					N = 40	$\sum f_i u_i = 5$

Let the assumed mean be (A) = 15

h = 6

$$\text{Mean} = A + h \frac{\sum f_i u_i}{N}$$

$$= 15 + 6 \left(\frac{5}{40} \right)$$

$$= 15 + 0.75$$

$$= 15.75$$

Section E

36. i. 8 coins

ii. Money in the piggy bank day wise 5, 10, 15, 20 ...

Money after 8 days = ₹ 180

iii. a. We can have at most 120 coins.

$$\frac{n}{2} [2(1) + (n - 1)1] = 120$$

$$n^2 + n - 240 = 0$$

Solving for n, we get, n = 15 as n ≠ -16

∴ Number of days = 15

OR

b. Total money saved = 120 × 5 = ₹ 600

37. i. Distance travelled by second bus = 7.2 km

∴ Total fare = 7.2 × 15 = ₹ 08

ii. Required distance = $\sqrt{(2 + 2)^2 + (3 + 3)^2}$

$$= \sqrt{4^2 + 6^2} = \sqrt{16 + 36} = 2\sqrt{13} \text{ km} \approx 7.2 \text{ km}$$

$$\begin{aligned}\text{iii. Required distance} &= \sqrt{(3+2)^2 + (2+3)^2} \\ &= \sqrt{5^2 + 5^2} = 5\sqrt{2} \text{ km}\end{aligned}$$

OR

Distance between B and C

$$= \sqrt{(3-2)^2 + (2-3)^2} = \sqrt{1+1} = \sqrt{2} \text{ km}$$

Thus, distance travelled by first bus to reach to B

$$= AC + CB = 5\sqrt{2} + \sqrt{2} = 6\sqrt{2} \text{ km} \approx 8.48 \text{ km}$$

and distance travelled by second bus to reach to B

$$= AB = 2\sqrt{13} \text{ km} = 7.2 \text{ km}$$

\therefore Distance of first bus is greater than distance of the cond bus, therefore second bus should be chosen.

$$38. \text{ i. Length } BD = AD - AB$$

$$= 10 - 2.5 = 8.5$$

ii. The length of ladder BC

In $\triangle BDC$

$$\cos \theta = \frac{\sqrt{3}}{2}$$

$$\Rightarrow \theta = 30^\circ$$

$$\sin 30^\circ = \frac{BD}{BC}$$

$$\Rightarrow \frac{1}{2} = \frac{8.5}{BC}$$

$$\Rightarrow BC = 2 \times 8.5 = 17 \text{ m}$$

iii. Distance between foot of ladder and foot of wall CD

In $\triangle BDC$

$$\cos 30^\circ = \frac{CD}{BC}$$

$$\Rightarrow \frac{\sqrt{3}}{2} = \frac{CD}{17}$$

$$\Rightarrow CD = 8.5\sqrt{3} \text{ m}$$

OR

If the height of pole and distance BD is doubled, then the length of the ladder is

$$\sin 30^\circ = \frac{BD}{BC}$$

$$\Rightarrow \frac{1}{2} = \frac{17}{BC}$$

$$\Rightarrow BC = 2 \times 17 = 34 \text{ m}$$